Display Adaptive 3D Content Remapping

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Abstract

Glasses-free automultiscopic displays are on the verge of becoming a standard technology in consumer products. These displays are capable of producing the illusion of 3D content without the need of any additional eyewear. However, due to limitations in angular resolution, they can only show a limited depth of field, which translates into blurred-out areas whenever an object extrudes beyond a certain depth. Moreover, the blurring is device-specific, due to the different constraints of each display. We introduce a novel display-adaptive light field retargeting method, to provide high-quality, blur-free viewing experiences of the same content on a variety of display types, ranging from hand-held devices to movie theaters. We pose the problem as an optimization, which aims at modifying the original light field so that the displayed content appears sharp while preserving the original perception of depth. In particular, we run the optimization on the central view and use warping to synthesize the rest of the light field. We validate our method using existing objective metrics for both image quality (blur) and perceived depth. The proposed framework can also be applied to retargeting disparities in stereoscopic image displays, supporting both dichotomous and non-dichotomous comfort zones.

Keywords: stereo, displays, automultiscopic, content retargeting.

1 1. Introduction

Within the last years, stereoscopic and automultiscopic dis-2 ³ plays have started to enter the consumer market from all an-4 gles. These displays can show three-dimensional objects that 5 appear to be floating in front of or behind the physical screen, 6 even without the use of additional eyewear. Capable of elec-7 tronically switching between a full-resolution 2D and a lower-8 resolution 3D mode, parallax barrier technology [1] is dominant 9 for hand-held and tablet-sized devices, while medium-sized dis-¹⁰ plays most often employ arrays of microlenses [2]. Although 11 most cinema screens today are stereoscopic and rely on addi-12 tional eyewear, large-scale automultiscopic projection systems ¹³ are an emerging technology [3]. Each technology has its own 14 particular characteristics, including field of view, depth of field, 15 contrast, resolution, and screen size. Counterintuitively, pro-16 duced content is usually targeted toward a single display con-17 figuration, making labor-intense, manual post-processing of the 18 recorded or rendered data necessary.

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Display-adaptive content retargeting is common practice for attributes such as image size, dynamic range (tone mapping), color gamut, and spatial resolution [4]. In order to counteract such accommodation-convergence mismatch of stereoscopic displays, stereoscopic disparity retargeting methods have recently been explored [5, 6, 7, 8, 9]. These techniques are successful in modifying the disparities of a stereo image pair so that visual discomfort of the observer is mitigated while preservnew ing the three-dimensional appearance of the scene as much as possible. Inspired by these techniques, we tackle the problem of 3D content retargeting for glasses-free light field (i.e. automultiscopic) displays. These displays exhibit a device-specific

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Figure 1: Our 3D content retargeting for a glasses-free lenticular display. Due to the limited depth of field of all light field displays, some objects in a 3D scene will appear blurred. Our remapping approach selectively fits the 3D content into the depth budget of the display, while preserving the perceived depth of the original scene. Top: actual photographs of the original and retargeted scenes, as seen on a Toshiba GL1 lenticular display. Notice the improvement in the blue bird or the legs of the green bird in the retargeted version. Middle: close-ups. Bottom: original and retargeted depths yielded by our method.

³² depth of field (DOF) that is governed by their limited angular ³³ resolution [10, 11]. Due to the fact that most light field dis-³⁴ plays only provide a low angular resolution, that is the number ³⁵ of viewing zones, the supported DOF is so shallow that virtual



Figure 2: Simulated views of the *three-birds* scene for three different displays. From left to right: Holografika HoloVizio C80 movie screen, desktop and cell phone displays. The last two displays fail to reproduce it properly, due to their intrinsic depth-of-field limitations. The insets plot the depth vs. cut-off frequency charts for each display.

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³⁶ 3D objects extruding from the physical display enclosure ap-³⁷ pear blurred out (see Figs. 1, left, and 2 for a real photograph ³⁸ and a simulation showing the effect, respectively). We propose ³⁹ here a framework that remaps the disparities in a 3D scene to ⁴⁰ fit the DOF constraints of a target display by means of an opti-⁴¹ mization scheme that leverages perceptual models of the human ⁴² visual system. Our optimization approach runs on the central ⁴³ view of an input light field and uses warping to synthesize the ⁴⁴ rest of the views.

46 Contributions. Our nonlinear optimization framework for
 47 3D content retargeting specifically provides the following con 48 tributions:

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49	• We propose a solution to handle the intrinsic trade-off
50	between the spatial frequency that can be shown and the
51	perceived depth of a given scene. This is a fundamental
52	limitation of automultiscopic displays (see Section 3).

We combine exact formulations of display-specific depth 53 of field limitations with models of human perception, to 54 find an optimized solution. In particular, we consider the 55 frequency-dependent sensitivity to contrast of the human 56 visual system, and the sensitivity to binocular disparity. 57 Based on this combination, a first objective term min-58 imizes the perceived luminance and contrast difference 59 between the original and the displayed scene, effectively 60 minimizing DOF blur, while a second term strives to pre-61 serve the perceived depth. 62

- We validate our results with existing state-of-the-art, objective metrics for both image quality and perceived depth.
- We show how our framework can be easily extended to the particular case of *stereoscopic* disparity, thus demonstrating its versatility.
- For this extension, we account for a non-dichotomous zone of viewing comfort which constitutes a more accurate model of discomfort associated with the viewing experience.

As a result of our algorithm, the depth of a given 3D scene r3 is modified to fit the DOF constraints imposed by the target ⁷⁴ display, while preserving the perceived 3D appearance and the ⁷⁵ desired 2D image fidelity (Figure 1, right).

Limitations. We do not aim at providing an accurate model 77 78 of the behavior of the human visual system; investigating all 79 the complex interactions between its individual components re-⁸⁰ mains an open problem as well, largely studied by both psy-81 chologists and physiologists. Instead, we rely on existing com-82 putational models of human perception and apply them to the ⁸³ specific application of 3D content retargeting. For this purpose, 84 we currently consider sensitivities to luminance contrast and 85 depth, but only approximate the complex interaction between ⁸⁶ these cues using a heuristic linear blending, which works well 87 in our particular setting. Using the contrast sensitivity func-⁸⁸ tion in our context (Section 4) is a convenient but conservative 89 choice. Finally, depth perception from motion parallax exhibits 90 strong similarities in terms of sensitivity with that of binocu-⁹¹ lar disparity, suggesting a close relationship between both [12]; 92 but existing studies on sensitivity to motion parallax are not as 93 exhaustive as those on binocular disparity, and therefore a reli-⁹⁴ able model cannot be derived yet. Moreover, some studies have 95 shown that, while both cues are effective, stereopsis is more rel-⁹⁶ evant by an order of magnitude [13]. In any case, our approach 97 is general enough so that as studies on these and other cues ad-⁹⁸ vance and new, more sophisticated models of human perception ⁹⁹ become available, they could be incorporated to our framework.

100 2. Related Work

Glasses-free 3D displays were invented more than a cen-102 tury ago, but even today, the two dominating technologies are 103 parallax barriers [1] and integral imaging [2]. Nowadays, the 104 palette of existing 3D display technologies, however, is much 105 larger and includes holograms, volumetric displays, multilayer 106 displays and directional backlighting among many others. State 107 of the art reviews of conventional stereoscopic and automul-108 tiscopic displays [14] and computational displays [15] can be 109 found in the literature. With the widespread use of stereoscopic 110 image capture and displays, optimal acquisition parameters and 111 capture systems [16, 17, 18, 19, 20], editing tools [21, 22], 112 and spatial resolution retargeting algorithms for light fields [23] ¹¹³ have recently emerged. In this paper, we deal with the prob-¹¹⁴ lem of depth remapping of light field information to the specific ¹¹⁵ constraints of each display.

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Generally speaking, content remapping is a standard ap-117 118 proach to adapt spatial and temporal resolution, contrast, col-¹¹⁹ ors, and sizes of images to a display having limited capabilities 120 in any of these dimensions [4]. For the particular case of dispar-121 ity remapping, Lang et al. [6] define a set of non-linear disparity 122 remapping operators, and propose a new stereoscopic warping 123 technique for the generation of the remapped stereo pairs. A 124 metric to assess the magnitude of perceived changes in binocu-125 lar disparity is introduced by Didyk et al. [8], who also inves-126 tigate the use of the Cornsweet illusion to enhance perceived 127 depth [24]. Recently, the original disparity metric has been fur-128 ther refined including the effect of luminance-contrast [9]. Kim 129 and colleagues [7] develop a a novel framework for flexible manipulation of binocular parallax, where a new stereo pair is cre-131 ated from two non-linear cuts of the EPI volume corresponding ¹³² to multi-perspective images [25]. Inspired by Lang and col-133 leagues [6], they explore linear and non-linear global remap-134 ping functions, and also non-linear disparity gradient compres-¹³⁵ sion. Here we focus on a remapping function that incorporates ¹³⁶ the specific depth of field limitations of the target display [26]. 137 Section 8 provides direct comparisons with some of these ap-138 proaches.

139 3. Display-specific Depth of Field Limitations

Automultiscopic displays are successful in creating convinc-140 141 ing illusions of three-dimensional objects floating in front and 142 behind physical display enclosures without the observer having ¹⁴³ to wear specialized glasses. Unfortunately, all such displays 144 have a limited depth of field which, just as in wide-aperture 145 photography, significantly blurs out-of-focus objects. The fo-146 cal plane for 3D displays is directly on the physical device. 147 Display-specific depth of field expressions have been derived ¹⁴⁸ for parallax barrier and lenslet-based systems [10], multilayer ¹⁴⁹ displays [11], and directional backlit displays [27]. In order to display an aliasing-free light field with any such device, fourdimensional spatio-angular pre-filters need to be applied before 151 152 computing the display-specific patterns necessary to synthesize 153 a light field, either by means of sampling or optimization. In 154 practice, these filters model the depth-dependent blur of the in-155 dividual displays and are described by a depth of field blur ap-156 plied to the target light field. Intuitively, this approach fits the ¹⁵⁷ content into the DOF of the displays by blurring it as necessary. 158 Figure 3 illustrates the supported depth of field of various auto-¹⁵⁹ multiscopic displays for different display sizes.

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¹⁶¹ Specifically, the depth of field of a display is modeled as the ¹⁶² maximum spatial frequency f_{ξ} of a diffuse plane at a distance ¹⁶³ d_0 to the physical display enclosure. As shown by previous ¹⁶⁴ works [10, 11], the DOF of parallax barrier and lenslet-based ¹⁶⁵ displays is given by



Figure 3: Depth of field for different display architectures and target displays. From left to right: cell phone (p = 0.09mm, $v_D = 0.35m$); desktop computer (p = 0.33mm, $v_D = 0.5m$); and widescreen TV (p = 0.53mm, $v_D = 2.5m$). For comparison purposes all depths of field are modeled for seven angular views.

$$\left| f_{\xi} \right| \le \begin{cases} \frac{f_0}{N_a}, & for |d_0| + (h/2) \le N_a h\\ (\frac{h}{(h/2) + |d_0|}) f_0, & otherwise \end{cases},$$
(1)

¹⁶⁶ where N_a is the number of angular views, d_0 is the distance ¹⁶⁷ to the front plane of the display (i.e. the parallax barrier or ¹⁶⁸ lenslet array plane), *h* represents the thickness of the display, ¹⁶⁹ $f_0 = 1/(2p)$, and *p* is the size of the view-dependent subpixels ¹⁷⁰ of the back layer of the display, making the maximum resolu-¹⁷¹ tion of the display at the front surface $f_{\xi} = f_0/N_a = 1/(2pN_a)$. ¹⁷² For multilayered displays, the upper bound on the depth of field ¹⁷³ for a display of *N* layers was derived by Wetzstein et al. [11] to ¹⁷⁴ be

$$\left| f_{\xi} \right| \le N f_0 \sqrt{\frac{(N+1)h^2}{(N+1)h^2 + 12(N-1)d_0^2}}.$$
 (2)

¹⁷⁵ Note that in this case d_0 represents the distance to the middle of ¹⁷⁶ the display, and *p* the pixel size of the layers.

178 It can be seen how depth of field depends on display pa-¹⁷⁹ rameters such as pixel size p, number of viewing zones N_a , $_{180}$ device thickness *h*, and number of layers *N* (for multilayer dis-181 plays), and thus varies significantly for different displays. It $_{182}$ also depends on the viewing distance v_D when expressed in cy-183 cles per degree. The above expressions can then be employed 184 to predict an image displayed on a particular architecture, in-185 cluding loss of contrast and blur. Figure 2 shows three sim-186 ulated views of the three-birds scene for three different dis-187 plays: a Holografika HoloVizio C80 movie screen (h = 100mm, 188 p = 0.765mm, $v_D = 6m$), a Toshiba automultiscopic monitor $_{189}$ ($h = 20, p = 0.33, v_D = 1.5$) and a cell-phone-sized display $_{190}$ (*h* = 6, *p* = 0.09, *v*_D = 0.35). The scene can be represented ¹⁹¹ in the large movie screen without blurring artifacts (left); how-192 ever, when displayed on a desktop display (middle), some areas ¹⁹³ appear blurred due to the depth-of-field limitations described ¹⁹⁴ above (see the blue bird). When seen on a cell-phone display 195 (right), where the limitations are more severe, the whole scene 196 appears badly blurred. In the following, we show how these 197 predictions are used to optimize the perceived appearance of ¹⁹⁸ a presented scene in terms of image sharpness and contrast, ¹⁹⁹ where the particular parameters of the targeted display are an 200 input to our method.

201 4. Optimization Framework

In order to mitigate display-specific DOF blur artifacts, we 202 ²⁰³ propose to scale the original scene into the provided depth bud-204 get while preserving the perceived 3D appearance as best as ²⁰⁵ possible. As detailed in Section 3, this is not trivial, since there ²⁰⁶ is an intrinsic trade-off between the two goals. We formulate 207 this as a multi objective optimization problem, with our objec-208 tive function made up of two terms. The first one minimizes 209 the perceived luminance and contrast difference between the 210 original and the displayed scene, for which display-specific ex-211 pressions of the displayable frequencies are combined with a 212 perceptual model of contrast sensitivity. The second term pe-213 nalizes loss in perceived depth, for which we leverage disparity 214 sensitivity metrics. Intuitively, the disparity term prevents the ²¹⁵ algorithm from yielding the obvious solution where the whole ²¹⁶ scene is flattened onto the display screen; this would guarantee ²¹⁷ perfect focus at the cost of losing any sensation of depth. The ²¹⁸ input to our algorithm is the depth map and the luminance im-219 age of the central view of the original light field, which we term $_{220} d_{orig}$ and L_{orig} , respectively. The output is a retargeted depth $_{221}$ map d, which is subsequently used to synthesize the retargeted 222 light field.

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specific frequency limitations by introducing spatially-varying, depth-dependent convolution kernels k(d). They are defined as Gaussian kernels whose standard deviation σ is such that frequencies above the cut-off frequency at a certain depth $f_{\mathcal{E}}(d)$ are reduced to less than 5% of its original magnitude. Although more accurate image formation models for defocus blur in scenes with occlusions can be found in the literature [28], their use is impractical in our optimization scenario, and we found the Gaussian spatially-varying kernels to give good results in practice. Kernels are normalized so as not to modify pixel *i* is:

$$k(d) = \frac{exp(-\frac{x_i^2 + y_i^2}{2(\sigma(d))^2})}{\sum_{j}^{K} \left(exp(-\frac{x_j^2 + y_j^2}{2(\sigma(d))^2})\right)}$$
(3)

where K is its number of pixels. The standard deviation σ is computed as:

$$\sigma(d) = \frac{\sqrt{-2\log(0.05)}}{2\pi p f_{\mathcal{E}}(d)} \tag{4}$$

with p being the pixel size in mm/pixel. 224 225

To take into account how frequency changes are perceived by a human observer, we rely on the fact that the visual system is more sensitive to near-threshold changes in contrast and less sensitive at high contrast levels [29]. We adopt a conservative approach and employ sensitivities at near-threshold levels as defined by the contrast sensitivity function (CSF). We follow the expression for contrast sensitivities ω_{CSF} proposed by Mantiuk et al. [30], which in turn builds on the model proposed by

Barten [31]:

$$\omega_{CSF}(l, f_l) = p_4 s_A(l) \frac{MTF(f_l)}{\sqrt{(1 + (p_1 f_l)^{p_2})(1 - e^{-(f_l/7)^2})^{-p_3}}},$$
 (5)

where *l* is the adapting luminance in $[cd/m^2]$, f_l represents the spatial frequency of the luminance signal in [cpd] and p_i are the fitted parameters provided in Mantiuk's paper¹. MTF (modulation transfer function) and s_A represent the optical and the luminance-based components respectively, and are given by:

$$MTF(f_l) = \sum_{k=1..4} a_k e^{-b_k f_l}$$
 (6)

$$s_A(l) = p_5 \left(\left(\frac{p_6}{l}\right)^{p_7} + 1 \right)^{-p_8}$$
(7)

where a_k and b_k can again be found in the original paper. Fig-227 ure 4 (left) shows contrast sensitivity functions for varying adap-228 tation luminances, as described by Equations 5-7. In our con-229 text we deal with complex images, as opposed to a uniform 230 field; we thus use the steerable pyramid [32] $\rho_S(\cdot)$ to decom-231 pose a luminance image into a multi-scale frequency represen-232 tation. The steerable pyramid is chosen over other commonly 233 used types of decomposition (e.g. Cortex Transform) since it Optimizing luminance and contrast: We model the display-234 is mostly free of ringing artifacts that can cause false masking 235 signals [30].

> Taking into account both the display-specific frequency limitations and the HVS response to contrast, we have the following final expression for the first term of our optimization:

$$\left\|\omega_{CSF}\left(\rho_{S}\left(L_{orig}\right)-\rho_{S}\left(\phi_{b}\left(L_{orig},d\right)\right)\right)\right\|_{2}^{2},$$
(8)

²³⁷ where ω_{CSF} , defined by Equation 5, are frequency-dependent weighting factors, and the operator $\phi_b(L, d) = k(d) * L$ models the total energy during convolution. As such, the kernel for a 239 the display-specific, depth-dependent blur (see Section 3 and Figure 3). Note that we omit the dependency of ω_{CSF} on (l, f_l) ²⁴¹ for clarity. Figure 5 (*left*) shows representative weights ω_{CSF} 242 for different spatial frequency luminance levels of the pyramid 243 for a sample scene.

> Preserving perceived depth: This term penalizes the perceived difference in depth between target and retargeted scene using disparity sensitivity metrics. As noted by different researchers, the effect of binocular disparity in the perception of depth works in a manner similar to the effect of contrast in the perception of luminance [8, 33, 34]. In particular, our ability to detect and discriminate depth from binocular disparity depends on the frequency and amplitude of the disparity signal. Human sensitivity to binocular disparity is given by the following equation [8] (see also Figure 4, right):

 $\omega_{BD}(a, f) = (0.4223 + 0.007576a + 0.5593log_{10}(f))$ (9) $+ 0.03742alog_{10}(f) + 0.0005623a^{2} + 0.7114log_{10}^{2}(f))^{-1}$

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¹sourceforge.net/apps/mediawiki/hdrvdp/



Figure 4: Thresholds and sensitivity values from which the weights for our optimization are drawn. Left: Contrast sensitivity functions. Right: Binocular disparity discrimination thresholds (thresholds are the inverse of sensitivities).

²⁴⁵ where frequency *f* is expressed in [cpd], *a* is the amplitude in ²⁴⁶ [arcmin], and ω_{BD} is the sensitivity in [arcmin⁻¹]. In a sim-²⁴⁷ ilar way to ω_{CSF} in Equation 8, the weights ω_{BD} account for ²⁴⁸ our sensitivity to disparity amplitude and frequency. Given this ²⁴⁹ dependency on frequency, the need for a multi-scale decom-²⁵⁰ position of image disparities arises again, for which we use a ²⁵¹ Laplacian pyramid ρ_L (·) for efficiency reasons, following the ²⁵² proposal by Didyk et al. [8]. Figure 5 (*right*), shows represen-²⁵³ tative weights ω_{BD} .

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The error in perceived depth incorporating these sensitivities is then modeled with the following term:

$$\left\|\omega_{BD}\left(\rho_L\left(\phi_{\upsilon}\left(d_{orig}\right)\right) - \rho_L\left(\phi_{\upsilon}\left(d\right)\right)\right)\right\|_2^2.$$
 (10)

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Given the viewing distance v_D and interaxial distance e, the period $\phi_v(\cdot)$ converts depth into vergence as follows:

$$\phi_{\upsilon}(d) = acos\left(\frac{\mathbf{v}_{\mathbf{L}} \cdot \mathbf{v}_{\mathbf{R}}}{\|\mathbf{v}_{\mathbf{L}}\| \|\mathbf{v}_{\mathbf{R}}\|}\right),\tag{11}$$

 $_{259}$ where vectors $\mathbf{v_L}$ and $\mathbf{v_R}$ are illustrated in Figure 6. The Lapla- $_{260}$ cian decomposition transforms this vergence into frequency- $_{261}$ dependent disparity levels.

Objective function: Our final objective function is a combination of Equations 8 and 10:

$$\arg\min_{d} \left(\mu_{DOF} \left\| \omega_{CSF} \left(\rho_{S} \left(L_{orig} \right) - \rho_{S} \left(\phi_{b} \left(L_{orig}, d \right) \right) \right) \right\|_{2}^{2} + \mu_{D} \left\| \omega_{BD} \left(\rho_{L} \left(\phi_{\nu} \left(d_{orig} \right) \right) - \rho_{L} \left(\phi_{\nu} \left(d \right) \right) \right) \right\|_{2}^{2} \right).$$
(12)

²⁶³ For multilayer displays, we empirically set the values of μ_{DOF} = ²⁶⁴ 10 and μ_D = 0.003, while for conventional displays μ_D = ²⁶⁵ 0.0003 due to the different depth of field expressions.

266 5. Implementation Details

We employ a large-scale trust region method [35] to solve Equation 12. This requires finding the expressions for the analytic gradients of the objective function used to compute the



Figure 5: Left: Weights ω_{CSF} (contrast sensitivity values) for different luminance spatial frequency levels for a sample scene (*birds*). Right: Weights ω_{BD} (inverse of discrimination threshold values) for different disparity spatial frequency levels for the same scene.



Figure 6: Computing vergence values. Vergence v_P of a point *P* depends on its position, the viewing distance v_D and the interaxial *e*. The corresponding disparity for *P* is $(v_P - v_F)$. *vd* refers to the viewing distance and d_P is the depth of point *P*.

²⁷⁰ Jacobian, which can be found in Annex A. The objective term ²⁷¹ in Equation 8 models a single view of the light field, i.e. the ²⁷² central view, in a display-specific field of view (FOV). Within ²⁷³ a moderate FOV, as provided by commercially-available dis-²⁷⁴ plays, this is a reasonable approximation; we obtain the rest of ²⁷⁵ the light field by warping. In the following, we describe this ²⁷⁶ and other additional implementation details.

278 **Sensitivity weights and target values:** The weights used 279 in the different terms, ω_{CSF} and ω_{BD} are pre-computed based on 280 the values of the original depth and luminance, d_{orig} and L_{orig} . 281 The transformation from d_{orig} to vergence, its pyramid decom-282 position and the decomposition of L_{orig} are also pre-computed. 283

Contrast sensitivity function: As reported by Mantiuk et al. [30], no suitable data exists to separate L- and M-cone sensitivity. Following their approach, we rely on the *achromatic* CSF using only luminance values.

Depth-of-field simulation: The depth-dependent image blur of automultiscopic displays is modeled as a spatially-varying convolution in each iteration of the optimization procedure. Due to limited computational resources, we approximate this expensive operation as a blend between multiple shift-invariant convolutions corresponding to a quantized depth map, making the process much more efficient. For all scenes shown in this paper, we use $n_c = 20$ quantized depth clusters.

²⁹⁸ **Warping:** View warping is orthogonal to the proposed re-²⁹⁹ targeting approach; we implement here the method described ³⁰⁰ by Didyk et al. [36], although other methods could be em-

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302 to large depth gradients at the limits of the field of view for 332 layer displays. The Toshiba panel has a native resolution of $_{303}$ each light field, we median-filter the depth and constrain depth $_{333}$ 3840 \times 2400 pixels with a specially engineered subpixel struc-304 values around the edges.

305 6. Retargeting for Stereoscopic Displays

One of the advantages of our framework is its versatility, 306 307 which allows to adapt it for display-specific disparity remap-³⁰⁸ ping of stereo pairs. We simply drop the depth of field term ³⁰⁹ from Equation 12, and incorporate a new term that models the 310 comfort zone. This is an area around the screen within which the 3D content does not create fatigue or discomfort in the 312 viewer in stereoscopic displays, and is usually considered as a 313 dichotomous subset of the fusional area. Although any comfort-314 zone model could be directly plugged into our framework, we 315 incorporate the more accurate, non-dichotomous model sug-316 gested by Shibata et al. [39]. This model provides a more ac-317 curate description of its underlying psychological and physio-318 logical effects. Additionally, this zone of comfort depends on the viewing distance v_D , resulting on different expressions for different displays, as shown in Figure 7. Please refer to Annex 321 B for details on how to incorporate the simpler, but less precise, 322 dichotomous model.

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Our objective function thus becomes:

$$\left\|\omega_{BD}\left(\rho_L\left(\phi_{\upsilon}\left(D_{orig}\right)\right) - \rho_L\left(\phi_{\upsilon}\left(d\right)\right)\right)\right\|_2^2 + \mu_{CZ} \left\|\varphi\left(d\right)\right\|_2^2, \quad (13)$$

where $\varphi(\cdot)$ is a function mapping depth values to visual discomfort:

$$\varphi(d) = \begin{cases} 1 - \frac{s_{far}}{v_{D} - d} - T_{far} & \text{for } d < 0\\ 1 - \frac{s_{near}}{v_{D} - d} - T_{near} & \text{for } d \ge 0 \end{cases}$$
(14)

 $_{325}$ the screen and s_{far} , s_{near} , T_{far} , and T_{near} are values obtained in $_{367}$ with the desktop inkjet printer influence the overall quality of 326 a user study carried out with 24 subjects.



Figure 7: Dichotomous (blue) and non-dichotomous (orange) zones of comfort for different devices. From left to right: cell phone ($v_D = 0.35m$), desktop computer ($v_D = 0.5m$) and wide-screen TV ($v_D = 2.5m$).

327 7. Results

We have implemented the proposed algorithm for differ-328 329 ent types of automultiscopic displays including a commercial 330 Toshiba GL1 lenticular-based display providing horizontal-only

301 ployed instead ([7, 37, 38]). To reduce warping artifacts due 331 parallax with nine discrete viewing zones, and custom multi- $_{334}$ ture that results in a resolution of 1280×800 pixels for each of 335 the nine views. Note that even a highly-engineered device such 336 as this suffers from a narrow depth of field due to the limited ³³⁷ angular sampling. We consider a viewing distance of 1.5 m for ³³⁸ the Toshiba display and 0.5 m for the multilayer prototypes.

> Figures 1 and 8 show results of our algorithm for the Toshiba 340 ³⁴¹ display. The target scenes have been originally rendered as light ₃₄₂ fields with a resolution of 9×9 , with a field of view of 10° . 343 Since the Toshiba display only supports horizontal parallax, we ³⁴⁴ only use the nine horizontal views for these examples. Note 345 how depth is compressed to fit the display's constraints in those 346 areas with visible loss of contrast due to blur (blue bird or far 347 away pins, for instance), while enhancing details to preserve the 348 perceived depth; areas with no visible blur are left untouched 349 (eyes of the green bird, for instance). This results into sharper 350 retargeted scenes that can be shown within the limitations of the 351 display. The remapping for the teaser image took two hours for $_{352}$ a resolution of 1024×768 , using our unoptimized Matlab code. 353

We have also fabricated a prototype multilayer display (Fig-354 355 ure 9). This display is composed of five inkjet-printed trans-356 parency patterns spaced by clear acrylic sheets. The size of $_{357}$ each layer is 60×45 mm, while each spacer has a thickness 358 of 1/8". The transparencies are conventional films for office 359 use and the printer is an Epson Stylus Photo 2200. This mul- $_{360}$ tilayer display supports 7 \times 7 views within a field of view of ³⁶¹ 7° for both horizontal and vertical parallax. The patterns are 362 generated with the computed tomography solver provided by ³⁶³ Wetzstein et al. [11]. Notice the significant sharpening of the ³⁶⁴ blue bird and, to a lesser extent, of the red bird. It should be 365 noted that these are lab prototypes: scattering, inter-reflections $_{324}$ where v_D is the distance from the viewer to the central plane of $_{366}$ between the acrylic sheets, and imperfect color reproduction ³⁶⁸ the physical results. In Figure 10, we show sharper, simulated ³⁶⁹ results for the *dice* scene for a similar multilayer display.

> We show additional results using more complex data sets, 371 372 with varying degrees of depth and texture, and different object 373 shapes and surface material properties. In particular, we use the Heidelberg light field archive², which includes ground-truth 375 depth information. The scenes are optimized for a three-layer ³⁷⁶ multilayer display, similar to the one shown in Figure 9. They 377 have been optimized for a viewing distance of 0.5 m and have $_{378}$ resolutions ranging from 768×768 to 1024×720 . The weights ³⁷⁹ used in the optimization are again $\mu_{DOF} = 10$ and $\mu_D = 0.003$. 380 Figure 11 shows the results for the *papillon*, *buddha2* and *statue* ³⁸¹ data sets. Our algorithm recovers most of the high frequency 382 content of the original scenes, lost by the physical limitations ³⁸³ of the display. The anaglyph representations allow to compare 384 the perceived depth of the original and the retargeted scenes

²http://hci.iwr.uni-heidelberg.de/HCI/Research/ LightField/lf_archive.php



Figure 8: Additional results for commercial lenticular display (actual photographs). Top row: depth map, perspective from left, and perspective from right for original scene. Bottom row: depth map and similar perspectives for the retargeted scene. The slight double-view of some of the pins in the left view is due to interview cross-talk in the Toshiba display.

385 (please refer to the supplementary material for larger versions ³⁸⁶ to ensure proper visualization). Figure 12 shows additional 387 views of the *buddha2* and *statue* light fields.



Figure 9: 3D content retargeting for multilayer light field displays (actual photographs). Even five attenuating layers (top) can only provide a limited depth of field for a displayed scene (bottom left). Our retargeting algorithm maps the multiview content into the provided depth budget (bottom right).

As shown in this section, our algorithm works well within a 389 wide range of displays and data sets of different complexities. 390 391 However, in areas of very high frequency content, the warp-³⁹² ing step may accumulate errors which end up being visible in ⁴⁰³ 8. Comparison to Other Methods ³⁹³ the extreme views of the light fields. Figure 13 shows this: 394 the *horses* data set contains a background made up of a texture ³⁹⁵ containing printed text. Although the details are successfully ³⁹⁶ recovered by our algorithm, the warping step cannot deal with ³⁹⁷ the extremely high frequency of the text, and the words appear ³⁹⁸ broken and illegible.

399

Finally, Figure 14 shows the result of applying our adapted 400 401 model to the particular case of stereo retargeting, as described



Figure 10: Results of simulations for a multilayer display (five layers). Top row: initial and retargeted depth. Middle row: initial and retargeted luminance. Bottom row: close-ups.

402 in Section 6.

Our method is the first to specifically deal with the par-404 405 ticular limitations of automultiscopic displays (depth vs. blur ⁴⁰⁶ trade-off), and thus it is difficult to directly compare with others. 407 However, we can make use of two recently published *objective* 408 computational metrics, to measure distortions both in the ob-⁴⁰⁹ served 2D image fidelity, and in the perception of depth. This 410 also provides an objective background to compare against exist-411 ing approaches for stereoscopic disparity retargeting, for which



Figure 11: Results for the *papillon* (top), *buddha2* (middle) and *statue* (bottom) data sets from the Heidelberg light field archive. For each data set, the top row shows the original scene, while the bottom row shows our retargeted result. From left to right: depth map, anaglyph representation, central view image, and selected zoomed-in regions. Notice how our method recovers most of the high frequency details of the scenes, while preserving the sensation of depth (larger versions of the anaglyphs appear in the supplementary material). Note: please wear anaglyph glasses with cyan filter on left and red filter on right eye; for an optimal viewing experience please resize the anaglyph to about 10 cm wide in screen space and view it at a distance of 0.5 m.

412 alternative methods do exist.

413



Figure 12: Additional non-central views of the retargeted *buddha2* and *statue* light fields, with corresponding close-ups.



Figure 13: Results for the *horses* data set from the Heidelberg light field archive. Very high frequencies that have been initially cut off by the display (green box) are successfully recovered by our algorithm (pink). However, subsequent warping can introduce visible artifacts in those cases, which progressively increase as we depart from the central view of the light field. This progression is shown in the bottom row (yellow boxes).

Metrics: We need to measure *both* observed 2D image 415 quality *and* resulting degradations in perceived depth. For im-416 age quality, numerous metrics exist. We rely on the HDR-VDP 417 2 calibration reports provided by Mantiuk and colleagues [30] 418 in their website³, where the authors compare quality predic-419 tions from six different metrics and two image databases: LIVE 420 [40] and TID2008 [41]. According to the prediction errors, re-421 ported as Spearman's correlation coefficient, multi-scale SSIM 422 (MS-SSIM, [42]) performs best across both databases for the 423 blurred image distortions observed in our application. The map-424 ping function we use, log(1-MS-SSIM), yields the highest cor-425 relation for Gaussian blur distortions.

426

Fewer metrics exist to evaluate distortions in depth. We use metric recently proposed by Didyk and colleagues to estimate the magnitude of the perceived disparity change between wo stereo images [8]. The metric outputs a heat map of the difmath differences between the original and the retargeted disparity maps



Figure 14: Retargeting for stereo content. *Left column:* Anaglyph and corresponding pixel disparity map of the original scene. For a common (around 0.5m) viewing distance on a desktop display, left and right images cannot be fused. *Right column:* Anaglyph and corresponding pixel disparity map of the retargeted scene. Images can now be fused without discomfort, and perception of depth is still present despite the aggressive depth compression. Note that the scales of the disparity maps are different for visualization purposes; the small inset shows the retargeted disparity map for the same scale as the original. Note: please wear anaglyph glasses with cyan filter on left and red filter on right eye; for an optimal viewing experience please resize the anaglyph to about 10 cm wide in screen space and view it at a distance of 0.5 m.

⁴³² in Just Noticeable Difference (JND) units.

433

Alternative Methods: There is a large space of linear and 434 435 non-linear global remapping operators, as well as of local ap-436 proaches. Also, these operators can be made more sophisti-437 cated, for instance by incorporating information from saliency 438 maps, or adding the temporal domain [6]. To provide some 439 context to the results of the objective metrics, we compare our 440 method with a representative subset of alternatives, including 441 global operators, local operators, and a recent operator based 442 on a perceptual model for disparity. In particular, we compare 443 against six other results using different approaches for stereo 444 retargeting: a linear scaling of pixel disparity (linear), a linear 445 scaling followed by the addition of bounded Cornsweet pro-446 files at depth discontinuities (Cornsweet [24])⁴, a logarith-⁴⁴⁷ mic remapping (log, see e.g. [6]), and the recently proposed ⁴⁴⁸ remapping of disparity in a perceptually linear space (*perc. lin*-449 ear [8]). For the last two, we present two results using different 450 parameters. This selection of methods covers a wide range from very simple to more sophisticated. 451

The linear scaling is straightforward to implement. For the bounded Cornsweet profiles method, where profiles are carefully controlled so that they do not exceed the given disparity bounds and create disturbing artifacts, we choose n = 5 levels as suggested by the authors. For the logarithmic remapping, we

452

³http://hdrvdp.sourceforge.net/reports/2.1/quality_live/ http:// hdrvdp.sourceforge.net/reports/2.1/quality_tid2008/

⁴In our tests, this consistently yielded better results than a naive application of unbounded Cornsweet profiles, as originally reported by Didyk and colleagues [24]

use the following expression, inspired by Lang et al. [6]:

$$\delta_o = K \cdot \log(1 + s \cdot \delta_i), \tag{15}$$

513

⁴⁵³ where δ_i and δ_o are the input and output pixel disparities, *s* is a ⁴⁵⁴ parameter that controls the scaling and *K* is chosen so that the ⁴⁵⁵ output pixel disparities fit inside the allowed range. We include ⁴⁵⁶ results for *s* = 0.5 and *s* = 5. Finally, for the perceptually lin-⁴⁵⁷ ear method, disparity values are mapped via transducers into a ⁴⁵⁸ perceptually linear space, and then linearly scaled by a factor *k*. ⁴⁵⁹ The choice of *k* implies a trade-off between the improvement in ⁴⁶⁰ contrast enhancement and how faithful to the original dispari-⁴⁶¹ ties we want to remain. We choose *k* = 0.75 and *k* = 0.95 as ⁴⁶² good representative values for both options respectively.

Comparisons: Some of the methods we compare against 464 465 (linear, Cornsweet and log) require to explicitly define a min-466 imum spatial cut-off frequency, which will in turn fix a certain target depth range. We run comparisons on different data sets and for a varied range of cut-off frequencies: For the birds 468 scene, where the viewing distance is $v_D = 1.5$ m, we test two 469 ⁴⁷⁰ cut-off frequencies: $f_{cpmm} = 0.12$ cycles per mm ($f_{cpd} = 3.14$ 471 cycles per degree), and $f_{cpmm} = 0.19$ ($f_{cpd} = 5.03$), the latter of 472 which corresponds to remapping to the depth range which of-473 fers the maximum spatial resolution of the display (see DOF 474 plots in Figure 16b). For the statue, papillon and buddha2 $_{475}$ scenes, optimized for a multilayer display with $v_D = 0.5$ m, $_{476}$ we set the frequencies to $f_{cpmm} = 0.4, 0.5$ and 1.1, respectively 477 (corresponding f_{cpd} = 3.49, 4.36 and 9.60). The frequencies 478 are chosen so that they yield a fair compromise between image 479 quality and perceived depth, given the trade-off between these 480 magnitudes; they vary across scenes due to the different spatial frequencies of the image content in the different data sets. 481 482

Figure 15 shows a comparison to the results obtained with 483 484 the other methods both in terms of image quality and of per-485 ceived depth for three different scenes from the Heidelberg data set (papillon, buddha2, and statue). Heat maps depict the error in perceived depth (in JNDs) given by Didyk et al.'s metric. Visual inspection shows that our method consistently leads to 489 less error in perceived depth (white areas mean error below the ⁴⁹⁰ 1 JND threshold). Close-ups correspond to zoomed-in regions ⁴⁹¹ from the resulting images obtained with each of the methods, ⁴⁹² where the amount of DOF blur can be observed (please refer ⁴⁹³ to the supplementary material for the complete images). Our ⁴⁹⁴ method systematically yields sharper images, even if it also pre-⁴⁹⁵ serves depth perception better. Only in one case, in the *statue* ⁴⁹⁶ scene, perceptually linear remapping yields sharper results, but ⁴⁹⁷ at the cost of a significantly higher error in depth perception, as 498 the corresponding heat maps show.

499

To better assess the quality of the deblurring of the retar-⁵⁰¹ geted images, Figure 16a shows the MS-SSIM metric for the ⁵⁰² different methods averaged over the scenes tested, together with ⁵⁰³ the associated standard error (we plot the absolute value of ⁵⁰⁴ log(1 - MS-SSIM)). We have added the result of the original ⁵⁰⁵ image, without any retargeting method applied (N for *none* in

⁵⁰⁶ the chart). Our method yields the best perceived image quality ⁵⁰⁷ (highest MS-SSIM value), and as shown in Figure 15, the low-⁵⁰⁸ est error in depth perception as well. This can be intuitively ex-⁵⁰⁹ plained by the fact that our proposed multi-objective optimiza-⁵¹⁰ tion (Eq. 12) explicitly optimizes *both* luminance and depth, ⁵¹¹ whereas existing algorithms are either heuristic or take into ac-⁵¹² count only one of the two aspects.

514 To further explore this image quality vs. depth percep-515 tion trade-off, we have run the comparisons for the *birds* scene 516 for two different cut-off spatial frequencies. Figure 16b shows 517 comparisons of all tested algorithms for the birds scene retar-518 geted for a lenslet-based display. For two of the methods, ours 519 and the perceptually linear remapping (with k = 0.75 and k =⁵²⁰ 0.95), defining this minimum spatial frequency is not necessary. 521 Error in depth for these is shown in the top row. For the other ⁵²² four methods (*linear*, Cornsweet, $log \ s = 0.5$, $log \ s = 5$), the 523 cut-off frequency needs to be explicitly defined: we set it to two ₅₂₄ different values of $f_{cpmm} = 0.12$ and $f_{cpmm} = 0.19$, which cor-525 respond to an intermediate value and to remapping the content 526 to the maximum spatial frequency of the display, respectively. 527 The resulting error in depth is shown in the middle and bottom ⁵²⁸ rows of Figure 16b. Error in perceived depth clearly increases 529 as the cut-off frequency is increased. The bar graph at the top ⁵³⁰ left of Figure 16b shows image quality results for $f_{cpmm} = 0.12$. ⁵³¹ Note that for $f_{cpmm} = 0.19$, the methods *linear*, *Cornsweet* and ⁵³² log yield perfectly sharp images (since we explicitly chose that ⁵³³ frequency to remap to the maximum resolution of the display), ⁵³⁴ but at the cost of large errors in perceived depth.

535 9. Conclusions and Future Work

Automultiscopic displays are an emerging technology with form factors ranging from hand-held devices to movie theater sections commercially successful implementations, however, face major technological challenges, including limited depth of field, resolution, and contrast. We argue that compelling multiview content will soon be widely available and tackle a crucial face part of the multiview production pipeline: display-adaptive 3D content retargeting. Our computational depth retargeting algotion fully, and deals with a part of the content production pipeline face that will become commonplace in the future.

As shown in the paper, there is an inherent trade-off in automultiscopic displays between depth budget and displayed spatial frequencies (blur): depth *has to* be altered if spatial frequenties in luminance are to be recovered. This is not a limitation of our algorithm, but of the targeted hardware (Figure 3). Our algorithm aims at finding the best possible trade-off, so that the inevitable depth distortions introduced to improve image qualties of blur (the cut-off frequency) in the retargeted scene depends of blur (the cut-off frequency) in the retargeted scene depends to the CSF. Should the user need to further control the amount of defocus deblurring, it could be added to the optimization in the form of constraints over the depth values according to the



Figure 15: Comparison against other methods for three different scenes from the Heidelberg light field archive. From top to bottom: *papillon* ($f_{cpmm} = 0.4$, $f_{cpd} = 3.49$), *buddha2* ($f_{cpmm} = 1.1$, $f_{cpd} = 9.60$), and *statue* ($f_{cpmm} = 0.5$, $f_{cpd} = 4.36$). Errors in depth are shown as heat maps (lower is better) according to the metric by Didyk and colleagues [8]; white areas correspond to differences below one JND. Viewing distance is 0.5 m.



Figure 16: (a) Comparison of average luminance quality (lack of blur) according to the MS-SSIM metric for all the data sets used in this comparisons (higher is better). (b) Comparison against other methods for the *birds* scene, for two different cut-off frequencies. Top row, from left to right: resulting image quality as predicted by MS-SSIM for $f_{cpmm} = 0.12$, and error in depth for the two methods that do not require providing a target depth range. Middle row: error in depth for the three methods requiring a target depth range, for a cut-off frequency $f_{cpmm} = 0.12$ ($f_{cpd} = 3.14$). The smaller image represents the depth vs. cut-off frequency function of the display, with the target depth range highlighted in yellow. Bottom row: same as middle row for a cut-off frequency $f_{cpmm} = 0.19$ ($f_{cpd} = 5.03$), corresponding to the maximum spatial frequency allowed by the display (flat region of the DOF function). Errors in depth are shown as heat maps (lower is better) according to Didyk et al's metric [8]; white areas correspond to differences below one JND. Note the intrinsic trade-off between image quality and depth perception for the methods requiring a specific target depth range: when remapping to the maximum spatial frequency of the display, error in perceived depth significantly increases. Viewing distance is 1.5 m.

561 corresponding DOF function.

562

⁵⁶³ We have demonstrated significant improvements in sharp-⁵⁶⁴ ness and contrast of displayed images without compromising

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A complete model of depth perception remains an open problem. One of the main challenges is the large number of cues that our brain uses when processing visual information, along with their complex interactions [43, 44]. A possible avenue of future work would be to extend the proposed optimization framework by including perceptual terms modeling human set sensitivity to accommodation, temporal changes in displayed images, sensitivity of depth perception due to motion parallax for the interplay between different perceptual cues. However, this is not trivial and will require significant advances in related set fields. Another interesting avenue of future work would be to set extend our optimization framework to deal with all the views in the light field, thus exploiting angular resolution.

59

We hope that our work will provide a foundation for the searching multiview content production pipeline and inspire oth searching the close relationship between light field acquisition, processing, and display limitations in novel yet unforeseen ways. We believe bringing the human visual system into the desearching the human visual system into the

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719 Appendix A. Objective Function and Analytical Derivatives

In this section we go through the mathematical expressions
 of the two terms of the objective function in detail. We also
 include their derivatives, necessary for computing the analytical
 Jacobian used in the optimization process.

724 Appendix A.1. Term 1: Optimizing Luminance and Contrast

This term, as shown in Equation (8) of the main text, has the following form:

$$T_{1} = \omega_{CSF} \left(\rho_{S} \left(L_{orig} \right) - \rho_{S} \left(\phi_{b} \left(L_{orig}, d \right) \right) \right)$$
(A.1)

⁷²⁵ Note that this expression yields a vector of length N_{pyr} (N_{pyr} ⁷²⁶ being the number of pixels in the pyramid $\rho_S (L_{orig})$ or

⁷²⁷ $\rho_S \left(\phi_b \left(L_{orig}, d \right) \right)$, which is a vector of differences with respect ⁷²⁸ to the target luminance L_{orig} , weighted by contrast sensitivity ⁷²⁹ values. This vector of errors thus contains the residuals that ⁷³⁰ lsqnonlin optimizes for the depth of field term. The weight-⁷³¹ ing factor μ_{DOF} is left out of this derivation for the sake of sim-⁷³² plicity, since it is just a product by a constant both in the objec-⁷³³ tive function term and in its derivatives. This is valid also for ⁷³⁴ the second term of the objective function.

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Since the multi-scale decomposition is a linear operation, we can write:

$$T_1 = \omega_{CSF} \left(M_S \cdot L_{orig} - M_S \cdot \phi_b \left(L_{orig}, d \right) \right)$$
(A.2)

where M_S is a matrix of size $N_{pyr} \times N_{im}$, N_{im} being the number of pixels in the luminance image L_{orig} . Substituting the blurring function $\phi_b(\cdot, \cdot)$ by its actual expression

$$\frac{\partial T_{1,i}}{\partial d} = \omega_{CSF,i} \left(-M_{S,i} \cdot (L_{orig} * \frac{\partial k(d)}{\partial d}) \right), \tag{A.3}$$

where $M_{S,i}$ is the *i*-th row of M_S . The derivative of the kernels k(d) is:

$$\frac{\partial k(d)}{\partial d} = \frac{\left(exp(-\frac{x_{j}^{2}+y_{i}^{2}}{2(\sigma(d))^{2}})\right)\left(\frac{(x_{i}^{2}+y_{i}^{2})4\sigma(d)\frac{\partial\sigma(d)}{\partial d}}{(2(\sigma(d))^{2})^{2}}\right)\sum_{j}^{K}\left[exp(-\frac{x_{j}^{2}+y_{j}^{2}}{2(\sigma(d))^{2}})\right]}{\left(\sum_{j}^{K}\left[exp(-\frac{x_{j}^{2}+y_{j}^{2}}{2(\sigma(d))^{2}})\right]\right)^{2}}$$
(A.4)
$$\frac{\sum_{j}^{K}\left[\left(exp(-\frac{x_{j}^{2}+y_{j}^{2}}{2(\sigma(d))^{2}})\right)\left(\frac{(x_{j}^{2}+y_{j}^{2})4\sigma(d)\frac{\partial\sigma(d)}{\partial d}}{(2(\sigma(d))^{2})^{2}}\right)\right]\left(exp(-\frac{x_{i}^{2}+y_{j}^{2}}{2(\sigma(d))^{2}})\right)}{\left(\sum_{j}^{K}\left[exp(-\frac{x_{j}^{2}+y_{j}^{2}}{2(\sigma(d))^{2}})\right]\right)^{2}}.$$

The derivative of the standard deviation σ is straightforward, knowing $\partial (f_{\xi}(d))/\partial d$. As described in the main text, the expression for $f_{\xi}(d)$ depends on the type of automultiscopic display. For a conventional display [10]:

$$f_{\xi}(d) = \begin{cases} \frac{f_0}{N_a}, & for |d| + (h/2) \le N_a h\\ (\frac{h}{(h/2) + |d|}) f_0, & otherwise \end{cases},$$
(A.5)

where N_a is the number of angular views, *h* represents the thickness of the display and $f_o = 1/(2p)$ is the spatial cut-off frequency of a mask layer with a pixel of size *p*. For multilayered displays, the upper bound on the depth of field for a display of *N* layers is [11]:

$$f_{\xi}(d) = N f_0 \sqrt{\frac{(N+1)h^2}{(N+1)h^2 + 12(N-1)d^2}}.$$
 (A.6)

The derivatives are as follows:

$$\frac{\partial f_{\xi}(d)}{\partial d} = \begin{cases} 0, & for |d| + (h/2) \le N_a h\\ (\frac{-hd/|d|}{((h/2) + |d|)^2}) f_0, & otherwise \end{cases}$$
(A.7)

for a conventional display and

$$\frac{\partial f_{\xi}(d)}{\partial d} = N f_0 \frac{12\sqrt{N+1}(N-1)hd}{((N+1)h^2 + 12(N-1)d^2)^{3/2}}.$$
 (A.8)

736 for a multilayered display.

737 Appendix A.2. Term 2: Preserving Perceived Depth

This term, introduced in Equation 10 of the main text, is modeled as follows:

$$T_{2} = \omega_{BD} \left(\rho_{L} \left(\phi_{\upsilon} \left(D_{orig} \right) \right) - \rho_{L} \left(\phi_{\upsilon} \left(d \right) \right) \right)$$
(A.9)

Again, since the multi-scale decomposition is a linear operation, we write:

$$T_{2} = \omega_{BD} \left(M_{L} \cdot \phi_{\upsilon} \left(D_{orig} \right) - M_{L} \cdot \phi_{\upsilon} \left(d \right) \right)$$
(A.10)

where M_L is a matrix of size $N_{dpyr} \times N_d$, N_d being the number of pixels in the depth map D_{orig} . Taking the derivative with respect to *d* yields the following expression for each element $T_{2,i}$ of the residuals vector for this term:

$$\frac{\partial T_{2,i}}{\partial d} = \omega_{BD,i} \left(-M_{L,i} \cdot \frac{\partial \phi_{\nu}\left(d\right)}{\partial d} \right), \tag{A.11}$$

where $M_{L,i}$ is the i - th row of M_L . As explained in the main text, $\phi_v(d)$ converts depth d_P of a point P into vergence v_P . This, given the viewing distance v_D and the interaxial distance e, is done using function $\phi_v(\cdot)$:

$$\phi_{\upsilon}(d) = acos\left(\frac{\mathbf{v}_{\mathbf{L}} \cdot \mathbf{v}_{\mathbf{R}}}{\|\mathbf{v}_{\mathbf{L}}\| \|\mathbf{v}_{\mathbf{R}}\|}\right), \qquad (A.12)$$

where vectors $\mathbf{v}_{\mathbf{L}}$ and $\mathbf{v}_{\mathbf{R}}$ have their origins in *P* and end in the eyes (please also see Figure 6 in the main text). Placing the coordinate origin in the center of the screen (z-axis normal to the screen, x-axis in the horizontal direction) we can rewrite the previous equation for a point $P = (x_i, y_i, d_i)$ as:

$$v_d = \phi_v(d) = acos\left(\frac{\kappa}{\sqrt{\eta}\sqrt{\zeta}}\right),$$
 (A.13)

738 where:

⁷⁴⁰ ⁷⁴⁰ ⁷⁴¹ $\eta = (x_L - x_i)^2 + (v_D - d_i)^2,$ ⁷⁴² ⁷⁴³ $\zeta = (x_R - x_i)^2 + (v_D - d_i)^2.$ ⁷⁴⁴

Finally, differentiating Equation A.13 with respect to depth:

$$\frac{\partial \phi_{\upsilon}(d)}{\partial d} = -\left(1 - \left(\frac{\kappa}{\sqrt{\eta}\sqrt{\zeta}}\right)^2\right)^{-1/2} \cdot \left(\frac{-2(\nu_D - d_i)\sqrt{\eta}\sqrt{\zeta} - \kappa\Psi(d_i)}{\eta\zeta}\right)^2$$

⁷⁴⁵ where $\Psi(d_i)$ is as follows:

$$\Psi(d_i) = -d_i(v_D - d_i)\eta^{-1/2}\zeta^{1/2} - d_i(v_D - d_i)\zeta^{-1/2}\eta^{1/2}$$

746 Appendix B. A Dichotomous Zone of Comfort

As explained in the paper, Equation B.1 describes our objective function for the simplified case of stereo remapping:

$$\left\|\omega_{BD}\left(\rho_L\left(\phi_{\upsilon}\left(D_{orig}\right)\right) - \rho_L\left(\phi_{\upsilon}\left(d\right)\right)\right)\right\|_2^2 + \mu_{CZ} \left\|\varphi\left(d\right)\right\|_2^2, \quad (B.1)$$

where $\varphi(\cdot)$ is a function mapping depth values to visual discomfort. To incorporate a dichotomous model (such as those shown in cyan in Figure 7 for different devices and viewing distances v_D), instead of the non-dichotomous model described in the paper (shown in orange in the same figure), we can define a binary indicator function, such as

$$\varphi_{dc}(d) = \begin{cases} 0 & \text{for } d_{comfort}^{min} \le d \le d_{comfort}^{max} \\ \infty & \text{otherwise} \end{cases}$$
(B.2)

For a practical, numerically-robust implementation, a smooth function that approximates Equation B.2 is preferable, ensuring C^1 continuity. Our choice for such a function is the Butterworth function which is commonly used as a low-pass filter in signal processing:

$$\varphi_{bf}(d) = 1 - \sqrt{\frac{1}{1 + (\gamma d)^{2s}}}$$
 (B.3)

 $_{747}$ where γ controls the position of the cut-off locations and *s* the $_{748}$ slope of such cut-offs.